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The meaning and consequences of star formation criteria in galaxy models with resolved stellar feedback

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ABSTRACT

We consider the effects of different criteria for determining where stars will form in gas on galactic scales, in simulations with high (1 pc) resolution, with explicitly resolved physics of Giant Molecular Cloud (GMC) formation and destruction, and stellar feedback from supernovae, radiation pressure, stellar winds and photoheating. We compare: (1) a self-gravity criterion (based on the local virial parameter and the assumption that self-gravitating gas collapses to high density in a single free-fall time), (2) a fixed density threshold, (3) a molecular-gas law, (4) a temperature threshold, (5) a requirement that the gas be Jeans unstable, (6) a criteria that cooling times be shorter than dynamical times and (7) a convergent-flow criterion. We consider all of these in both a Milky Way (MW)-like and high-density (starburst or high-redshift) galaxy. With feedback present, all models produce *identical* integrated star formation rates (SFRs), in good agreement with the Kennicutt relation; without feedback all produce orders-of-magnitude excessive SFRs. This is totally dependent on feedback and independent of the star formation (SF) law, even if the ‘local’ collapse efficiency is 100 per cent. However, the predicted spatial and density distribution depend strongly on the SF criteria. Because cooling rates are generally fast within galaxy discs, and gas is turbulent, criteria (4)–(7) are very ‘weak’ and spread the SF uniformly over most of the disc (down to densities $n \sim 0.01\text{--}0.1\text{ cm}^{-3}$). A molecular criterion (3) localizes to slightly higher densities, but still a wide range; for metallicity near solar, it is almost identical to a fixed density threshold at $n \sim 1\text{ cm}^{-3}$ (well below the mean density in the central MW or starburst systems). A fixed density threshold (2) can always select the highest resolved densities, but must be adjusted both for simulation resolution and individual galaxy properties – the same threshold that works well in a MW-like simulation will select nearly all gas in a starburst. Binding criteria (1) tend to adaptively select the largest local overdensities, independent of galaxy model or resolution, and automatically predict clustered SF. We argue that this SF model (possible with other secondary criteria) is most physically motivated and presents significant numerical advantages in simulations with a large dynamic range.

Key words: galaxies: active – galaxies: evolution – galaxies: formation – cosmology: theory.

1 INTRODUCTION

Modelling star formation (SF) accurately is critical for any simulation of galaxy formation. However, cosmological and galaxy-scale simulations still cannot hope to resolve the spatial and density scales on which SF actually occurs. As a result, simple ‘recipes’ must be

applied. For example, models typically impose some ‘local Schmidt law’, where gas forms stars at a rate that scales as some power of the density; if the star formation rate (SFR) per local free-fall time $t_{\text{ff}} \propto 1/\sqrt{G\rho}$ were constant, this would be $\dot{\rho}_* \propto \rho/t_{\text{ff}} \propto \rho^{1.5}$, although in principle any other parameters can be used.

Usually, applying these models alone would artificially spread SF among all the gas in the simulation, even cosmologically pristine material at high temperatures. So some additional criteria or restrictions must be included. Most commonly, this amounts to a simple density threshold: $n \gtrsim 0.1\text{ cm}^{-3}$ in many cosmological

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simulations. This is not to say such low-density material directly forms stars: rather, this corresponds crudely to densities where the thermal instability sets in, so some unresolved fraction of the material (which goes into the subgrid scaling above) will be able to form stars. Other common requirements include restricting SF to gas which is below some temperature, or Jeans unstable, or in convergent flows, or which has a short cooling time. Recently, various studies have considered molecular criteria: using some combination of density and metallicity to estimate a subgrid molecular gas fraction and restricting SF to the ‘molecular’ gas (Robertson & Kravtsov 2008; Kuhlen et al. 2011).

These criteria are not trivial. SF is observed to be highly clustered under essentially all conditions (Lada & Lada 2003, and references therein), and without some criteria such as those above, this is not captured in simulations. This does not just mean that stars are forming in the wrong places. ‘Smearing out’ SF over the disc dramatically suppresses the effects of stellar feedback (Governato et al. 2010). Massive star clusters allow for, e.g., overlapping supernovae (SNe) ‘bubbles’ that can expand much more efficiently than individual SNe remnants. They also concentrate feedback ‘where it is needed’, i.e. it preferentially acts in the dense, star-forming gas. Strong radiation pressure effects arise when photons are trapped in optical thick regions around embedded clusters (Hopkins, Quataert & Murray 2011). And spreading out SF leads to spurious geometric cancellation between feedback sources. Without a sufficiently strict minimum SF criterion, the ability of the gas to form realistic phase structure (Saitoh et al. 2008), or blow winds that regulate its baryon content (Governato et al. 2010) and form realistic discs (Governato et al. 2004; Pontzen & Governato 2012) can be fundamentally altered.

Unfortunately, in practice the physical interpretation of these criteria often depends both on the resolved dynamic range of the simulation and on the mean properties of the galaxies being simulated, and to obtain similar results they must be numerically adjusted accordingly.

However, it is increasingly clear that the interstellar medium (ISM) is governed by supersonic turbulence over a wide range of scales. Consider, then, a locally self-gravitating region of the ISM ‘supported’ by turbulence. In the absence of some feedback disrupting it or ‘pumping’ the dispersion, the turbulent support will be damped in a single crossing time; as a result the region will collapse to arbitrarily high densities in about one free-fall time. This is true even if the energy of contraction maintains a constant virial equilibrium at each radius (Hopkins 2013). At sufficiently high densities, *eventually* all of the above criteria must be met; so as long as the SFR increases with density, eventually an order-unity fraction of the gas will be consumed into stars. So – in the absence of some self-regulation – the time-averaged SFR should be $\dot{\rho}_* \approx \rho/t_{\text{collapse}} \sim \rho/t_{\text{ff}}$ *regardless* of the ‘true’ local SF criteria/law. This is precisely what is seen in detailed simulations of turbulent media, in the absence of ‘pumping’ to unbind collapsing regions (Ballesteros-Paredes et al. 2011; Padoan & Nordlund 2011; Padoan, Haugbølle & Nordlund 2012).

We stress that this does not mean the total SFR, even within a dense parcel of gas, will actually be as large as $\rho_{\text{gas}}/t_{\text{ff}}$. If feedback *is* present, it can self-regulate. As soon as some gas turns into stars, feedback can act and disrupt the bound material, terminating the SF locally and suppressing nearby SF even in the dense gas. In such a model, however, the ‘net’ efficiency is actually predicted self-consistently from the feedback model, rather than imposed by the subgrid model (by, say, forcing some by hand low normalization of $\dot{\rho}_*(\rho)$).

Of course, if a simulation resolves a bound region, then this collapse will be followed self-consistently. What we require is a mechanism to treat further collapse, where it would occur, below our resolution limit. In this Letter, we propose a simple adaptive self-gravity criterion for SF in galaxy-scale and cosmological simulations, motivated by the numerical simulations above. We compare it to other common criteria in the literature, and examine the implications for the equilibrium SFRs and both the predicted spatial and density distributions of SF in different galaxy environments.

2 A SIMPLE SELF-GRAVITY CRITERION

On some scale δr , self-gravity requires $\sigma_{\text{eff}}^2 + c_s^2 < \beta G M (<\delta r)/\delta r$, where σ_{eff} includes the contributions from both rotational and random motions and β is an appropriate constant that depends on the internal structure in δr . In practice, the gas of interest is always highly supersonic in our simulations (and in observations), so we can ignore the c_s term here. We then obtain the usual virial parameter

$$\alpha \equiv \sigma_{\text{eff}}^2 \delta r / \beta G M (<\delta r). \quad (1)$$

To determine *local* binding, we wish to describe α in the limit where δr is small. Then $M(<\delta r) = (4\pi/3) \bar{\rho} \delta r^3$, where $\bar{\rho}$ is the average density in δr , and $\sigma_{\text{eff}} \rightarrow \frac{\delta v}{\delta r} \delta r$, or more formally

$$\sigma_{\text{eff}}^2 = \beta_v (|\nabla \cdot \mathbf{v}|^2 + |\nabla \times \mathbf{v}|^2) \delta r^2 \equiv \left(\frac{\delta v}{\delta r} \right)^2 \delta r^2. \quad (2)$$

Here, the $\nabla \cdot \mathbf{v}$ term accounts for the local radial velocity dispersion and inflow/outflow motions, while the $\nabla \times \mathbf{v}$ term accounts for internal rotational/shear and tangential dispersion. The β_v term depends on the internal structure again but is close to unity.

Combining these terms, we can derive the formally resolution-independent criterion:

$$\alpha \equiv \beta' \frac{|\nabla \cdot \mathbf{v}|^2 + |\nabla \times \mathbf{v}|^2}{G \rho} < 1, \quad (3)$$

where $\beta' \approx 1/2$ collects the order-unity terms above. This prefactor depends on the internal mass profile and velocity structure, but only weakly, for example, a Plummer sphere or Hernquist (1990) mass distribution with pure isotropic, rotationally supported or constant velocity gradient orbits the range $\beta' \approx 0.5\text{--}0.6$.

This criterion is well behaved in the local limit and does not explicitly depend on any numerical parameters of the simulation (spatial or mass resolution), nor does it require inserting any ‘ad hoc’ threshold or normalization criterion. Because it depends only on the local velocity gradient and density, it is trivial to implement in either Lagrangian (smoothed particle hydrodynamics, SPH) or Eulerian (grid) codes (as compared to an explicit evaluation of the binding criterion over some *resolved* scalelength, which requires a neighbour search, and can be prohibitively expensive in certain situations).

Implicitly, the velocity gradients and average density are always evaluated at the scale of the resolution limit. If going to higher resolution would change these quantities, then of course the criterion would give a different result (but as a consequence of the physical, not numerical, difference).

3 THE SIMULATIONS

The simulations used here are described in detail in Hopkins et al. (2011, hereafter Paper I, see section 2 and tables 1–3) and Hopkins,

Quataert & Murray (2012a, hereafter Paper II, see section 2). We briefly summarize the most important properties here. The simulations were performed with the parallel TreeSPH code GADGET-3 (Springel 2005). They include stars, dark matter and gas, with cooling, shocks, SF and stellar feedback.

3.1 Star formation criteria

SF is allowed only in gas that meets some set of criteria, for example in density or temperature. Within the gas that is flagged as ‘star forming’, our standard model assumes $\dot{\rho}_* = \epsilon \rho / t_{\text{ff}}$, where t_{ff} is the free-fall time and ϵ is some efficiency. Unless otherwise specified, we set $\epsilon = 0.015$, to match the average observed efficiency in dense gas (e.g. Krumholz & Tan 2007, and references therein).

There are several criteria that can be imposed to determine the gas allowed to form stars, which are as follows.

(1) *Self-gravity*. We require a region to be locally self-gravitating as described in Section 2, i.e. $\alpha < 1$. But these regions are assumed to collapse in a single free-fall time, so $\epsilon = 1$ (this approximates the results in individual cloud simulations of Padoan et al. 2012).

(2) *Density*. SF is allowed above a simple density threshold $n > n_0$, where we adopt $n_0 = 100 \text{ cm}^{-3}$ to ensure that this selects only overdense gas inside of typical Giant Molecular Clouds (GMCs).

(3) *Molecular gas*. We calculate the molecular fraction f_{H_2} of all gas as a function of the local column density and metallicity following Krumholz & Gnedin (2011) and allow SF only from the molecular gas (i.e. multiply ϵ by f_{H_2}).

(4) *Temperature*. We allow SF only below a minimum temperature $T < T_{\text{min}}$. Here, we adopt $T_{\text{min}} = 100 \text{ K}$ (chosen to approach the minimum temperatures the simulation can resolve). At these temperatures, we expect this to be very similar to criterion (2).

(5) *Jeans instability*. We require the gas be locally Jeans unstable below the resolution limit: $c_s < h_{\text{sml}} \sqrt{4\pi G \rho}$ (h_{sml} is the SPH smoothing length). Given the Lagrangian nature of the simulations, this translates to a temperature $T \lesssim 100 \text{ K} (m_i/300 M_{\odot}) / (h_{\text{sml}}/10 \text{ pc})$ where m_i is the particle mass.

(6) *Converging flows*. SF is allowed only in convergent flows, i.e. where $\nabla \cdot \mathbf{v} < 0$.

(7) *Rapid cooling*. We allow SF only in regions where the cooling time is less than the dynamical time, $t_{\text{cool}} < 1/\sqrt{G\rho}$.

3.2 Cooling and feedback

Gas follows an atomic cooling curve with additional fine structure cooling to $\sim 10 \text{ K}$. At all the scales we resolve, the cooling time in dense gas tends to be much shorter than the dynamical time for any temperatures $T \gtrsim 10^4 \text{ K}$ where the thermal pressure would be significant, and the minimum resolved scales are significantly larger than the sonic length. As a result, varying the cooling curve shape, magnitude or metallicity dependence within an order of magnitude has no significant effect on any of our conclusions.

Stellar feedback is included from a variety of mechanisms.

(1) *Local momentum-driven winds from radiation pressure, SNe and stellar winds*. Gas within a GMC (identified with an on-the-fly friends-of-friends algorithm) receives a direct momentum flux from the stars in that cluster/clump. The momentum flux is $\dot{P} = \dot{P}_{\text{SNe}} + \dot{P}_{\text{w}} + \dot{P}_{\text{rad}}$, where the separate terms represent the direct momentum flux of SNe ejecta, stellar winds and radiation pressure. The first two are directly tabulated for a single stellar population as a function of age and metallicity Z and the flux is directed away from the stellar centre. Because this is interior to clouds, the systems

are always optically thick, so the latter is approximately $\dot{P}_{\text{rad}} \approx (1 + \tau_{\text{IR}}) L_{\text{incident}}/c$, where $1 + \tau_{\text{IR}} = 1 + \Sigma_{\text{gas}} \kappa_{\text{IR}}$ accounts for the absorption of the initial ultraviolet/optical flux and multiple scatterings of the infrared (IR) flux if the region is optically thick in the IR (with Σ_{gas} calculated for each particle).

(2) *SN shock heating*. Gas shocked by SNe can be heated to high temperatures. We tabulate the Types I and II SNe rates from Mannucci, Della Valle & Panagia (2006) and STARBURST99, respectively, as a function of age and metallicity for all star particles and stochastically determine at each time step if an SN occurs. If so, the appropriate mechanical luminosity is injected as thermal energy in the gas within a smoothing length of the star particle.

(3) *Gas recycling and shock heating in stellar winds*. Gas mass is returned to the ISM from stellar evolution, at a rate tabulated from SNe and stellar mass-loss (integrated fraction ≈ 0.3). The SNe heating is described above. Similarly, stellar winds are assumed to shock locally and inject the appropriate tabulated mechanical luminosity $L(t, Z)$ as a function of age and metallicity into the gas within a smoothing length.

(4) *Photoheating of H II regions and photoelectric heating*. We also tabulate the rate of production of ionizing photons for each star particle; moving radially outwards from the star, we then ionize each neutral gas particle (using its density and state to determine the necessary photon number) until the photon budget is exhausted. Ionized gas is maintained at a minimum $\sim 10^4 \text{ K}$ until it falls outside an H II region. Photoelectric heating is followed in a similar manner using the heating rates from Wolfire et al. (1995).

(5) *Long range radiation pressure*. Photons which escape the local GMC (not accounted for in 1) can be absorbed at larger radii. Knowing the intrinsic Spectral Energy Distribution (SED) of each star particle, we attenuate integrating the local gas density and gradients to convergence. The resulting ‘escaped’ SED gives a flux that propagates to large distances, and can be treated in the same manner as the gravity tree to give the local net incident flux on a gas particle. The local absorption is then calculated integrating over a frequency-dependent opacity that scales with metallicity, and the radiation pressure force is imparted.

Details and numerical tests of these models are discussed in Paper II. All energy, mass and momentum-injection rates are taken as-is from the stellar population models in STARBURST99, assuming a Kroupa (2002) IMF, without any free parameters. Subtle variations in the implementation do not make significant differences to our conclusions. Most important, we do *not* ‘turn off’ or otherwise alter any of the cooling or hydrodynamics of the gas.

3.3 Galaxy models

We implement the model in two distinct initial disc models, chosen to span a wide range in ISM densities. Each has a bulge, stellar and gaseous disc, halo, and central black hole (BH; although to isolate the role of stellar feedback, models for BH growth and feedback are disabled). At our standard resolution, each model has $\sim 0.3\text{--}1 \times 10^8$ total particles, giving particle masses of $\sim 500 M_{\odot}$ and typical $\sim 5 \text{ pc}$ smoothing lengths in the dense gas,¹ and are run for a few orbital times each. The disc models include the following.

¹ Smoothing lengths are set adaptively as in Springel & Hernquist (2002), with an approximately constant 64 neighbours enclosed within the smoothing kernel.

(1) Milky Way (MW). A MW-like galaxy, with with baryonic mass $M_{\text{bar}} = 7.1 \times 10^{10} M_{\odot}$ (gas $m_{\text{g}} = 0.9 \times 10^{10} M_{\odot}$, bulge $M_{\text{b}} = 1.5 \times 10^{10} M_{\odot}$, the remainder in a stellar disc m_{d}) and halo mass $M_{\text{halo}} = 1.6 \times 10^{12} M_{\odot}$. The gas (stellar) scalelength is $h_{\text{g}} = 6.0$ kpc ($h_{\text{d}} = 3.0$). At standard resolution, gas particles and new stars have mass $m \approx 500 M_{\odot}$ and the force softening $\epsilon \approx 4$ pc.

(2) HiZ/Starburst. A massive starburst disc with densities typical of the central couple kpc in low- z galaxy mergers, or the larger scale ISM in star-forming galaxies at $z \sim 2-4$. Here, $M_{\text{halo}} = 1.4 \times 10^{12} M_{\odot}$ and baryonic ($M_{\text{bar}}, m_{\text{b}}, m_{\text{d}}, m_{\text{g}}$) = (10.7, 0.7, 3, 7) $\times 10^{10} M_{\odot}$ with scalelengths ($h_{\text{d}}, h_{\text{g}}$) = (1.6, 3.2) kpc.

4 RESULTS AND DISCUSSION

Fig. 1 shows the total SFR versus time for the models, with feedback enabled and disabled. We immediately see that the total SFR, hence the *net* SF efficiency, is almost totally independent of the SF criteria. However, it depends dramatically on feedback. With feedback on, the global SFR is $\dot{M}_{*} \sim 0.02 M_{\text{gas}}/t_{\text{dyn}}$, in agreement with

observations. Without feedback, it is $\dot{M}_{*} \sim 0.5 M_{\text{gas}}/t_{\text{dyn}}$.² Regardless of *how* mass turns into stars, a certain feedback strength, hence, mass in young stars, is needed to inject enough momentum to offset dissipation and prevent runaway collapse. Because cooling is rapid, the galaxy can always find a way to get ‘enough’ gas to the relevant densities/temperatures/binding criteria – at which point the SFR is a function of feedback efficiency alone. This is discussed in much greater detail in Paper I, where we show that, for example, changing the local SF law (efficiencies, power-law indices or density thresholds) makes no difference here, but changing the feedback strength directly changes the net efficiency. Without explicit feedback models, a local SF model that turned self-gravitating gas into stars with an efficiency ~ 1 would grossly overproduce observed SFRs; however, once feedback is included, the *mean* SF efficiency even in dense gas is a self-regulating quantity and we can safely consider such a prescription.³

The SF criteria does, however, affect the spatial and density distribution of SF in each model, shown in Figs 2 and 3. With arbitrarily high resolution, we would ideally want all the SF to be highly spatially clustered, and concentrated in absolute densities of $\gtrsim 10^6 \text{ cm}^{-3}$. Resolution limits mean this cannot be realized; the ‘next-best’ aim of these SF criteria is to identify the highest *local* overdensities and highest resolvable densities, which will contain subregions that collapse further, and associate SF with those regions.

Our proposed self-gravity criterion (1) adaptively selects the overdense regions in all galaxy models, giving a realistic ‘clumpy’ and clustered morphology for the SF. In the HiZ model in particular, it is able to associate SF with a number of small subclumps in the central regions, with densities $\gtrsim 10^4 \text{ cm}^{-3}$. (Note that the apparent ‘bimodality’ here is artificial, caused by a bottleneck at the highest densities allowed by our numerical resolution.)

A pure density criterion (2) works well when the threshold density is much larger than the background mean; however, it qualitatively changes character when the threshold falls below the mean density (the central regions of the HiZ model). Then, obviously, the SF becomes ‘smeared’ uniformly across all the gas, defeating the purpose of a density threshold in the first place. This is clear in the morphology in Fig. 2, where the ‘clumps’ previously evident have been largely ‘smeared out’ by more extended SF. Likewise in Fig. 3, the SFR is dominated by gas near the threshold density, even though it is clear that densities up to 4 dex larger can be resolved. A number of authors have shown that this leads to unphysical distributions of stars and SF, and can artificially suppress the efficiency of feedback as well (see Section 1). We stress that at least some of the cases here cannot simply be resolved by raising the threshold further: for example, in simulating galaxy nuclei, the minimum density any clump must have simply to avoid tidal disruption (a clear requirement for SF) scales is $\propto r^{-3}$, where r is the distance to the BH. Thus, properly

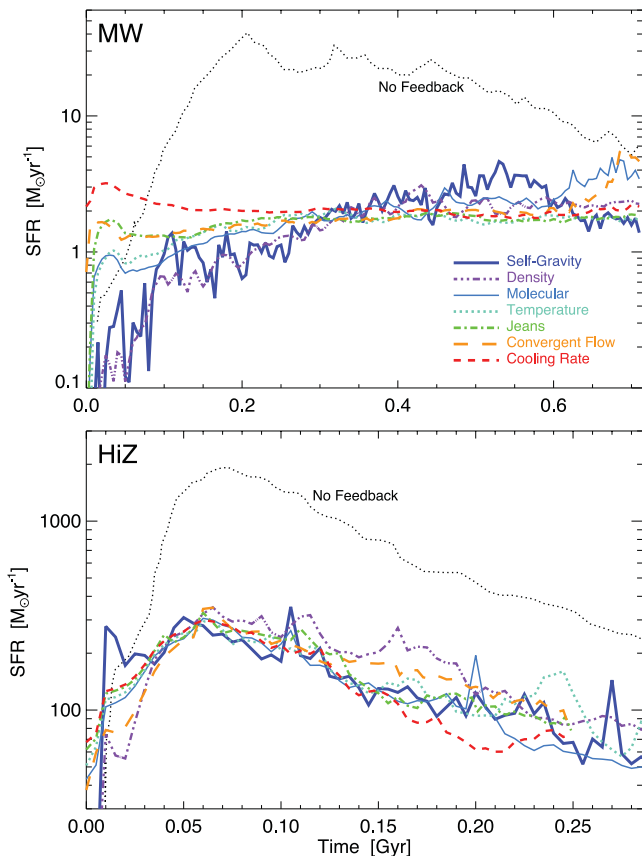


Figure 1. SFR versus time for the simulations with different SF prescriptions (as labelled), in the MW-like (top) and starburst/HiZ (bottom) disc models. The SF prescription has no effect on the actual SFRs (model differences, after the first couple dynamical times where non-equilibrium effects appear, are consistent with random variation). With realistic stellar feedback models, the SFR is entirely set by feedback (the mass in young stars is needed to prevent runaway collapse). With no feedback, SF efficiencies are extremely large (SFRs much larger than observed); with feedback, the SFRs agree well with observations in both models. In particular, despite having an instantaneous, local efficiency $\epsilon = 1$ in bound clouds, the actual average efficiency (ϵ) of the ‘self-gravity’ model is a realistic $\sim 1-5$ per cent.

² The apparent ‘convergence’ of the feedback and no feedback runs at late times occurs because the no feedback runs exhaust all their gas in just a few dynamical times. Thus, the SFR declines in absolute terms, even though it remains fixed in units of $M_{\text{gas}}/t_{\text{dyn}}$. This is shown explicitly in Papers I and II. We also refer interested readers to Paper I, fig. 11 for an explicit comparison of the simulations and the observed Schmidt–Kennicutt relation.

³ In Paper II, we examine how different feedback mechanisms individually affect the SF efficiency. In the lower density regime typical of the MW-like model, the dominant mechanism is a combination of photoionization heating (and resulting warm gas pressure) and the momentum injection in overlapping SNe explosions. In the higher density regime of the HiZ model, it is predominantly radiation pressure on dusty gas from the nearby Eddington-limited starburst.

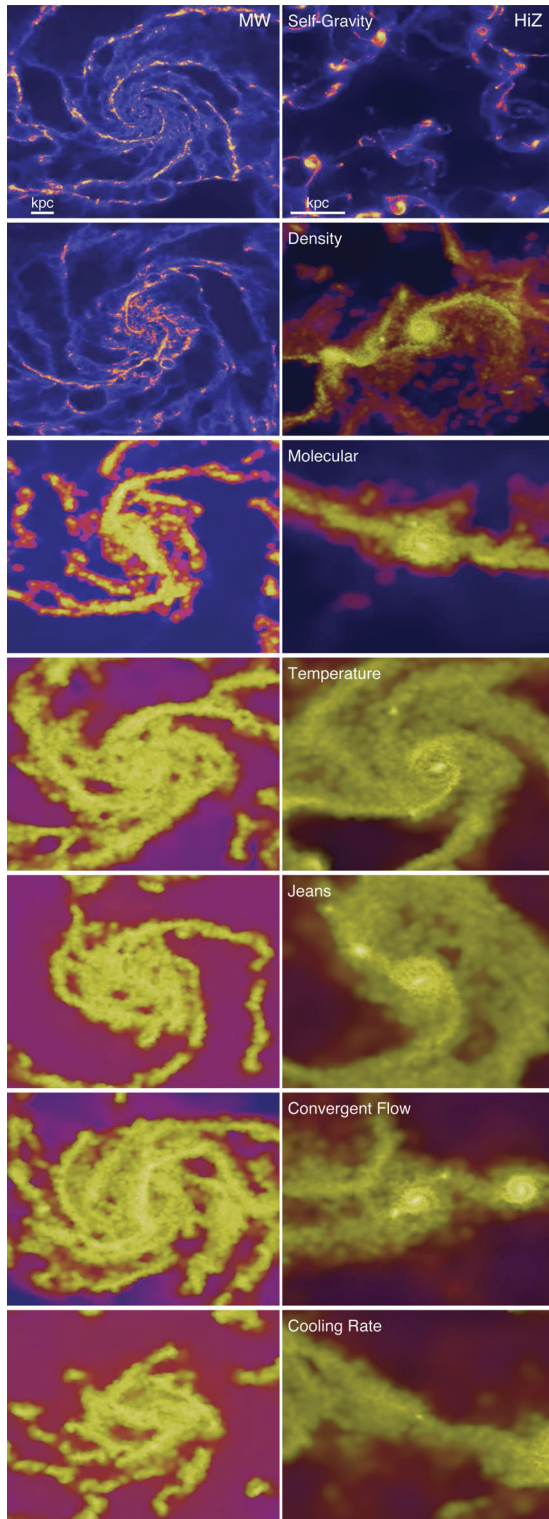


Figure 2. Gas surface density (intensity), with star-forming regions colour-coded as red–yellow (with increasing specific SFR). The *distribution* of SF varies with SF law. Local binding criteria select locally overdense regions in all cases. A fixed density threshold works well for most of the MW disc, but fails in the central, high- ρ regions of the HiZ model (where the mean density is above threshold). A molecular law works reasonably well in the outer regions of the MW model, but ‘smears’ SF among a much wider range of gas in spiral arms; in the HiZ/starburst nucleus model it identifies all gas as molecular. Temperature, Jeans stability, cooling rate and convergent-flow criteria select gas at nearly all densities.

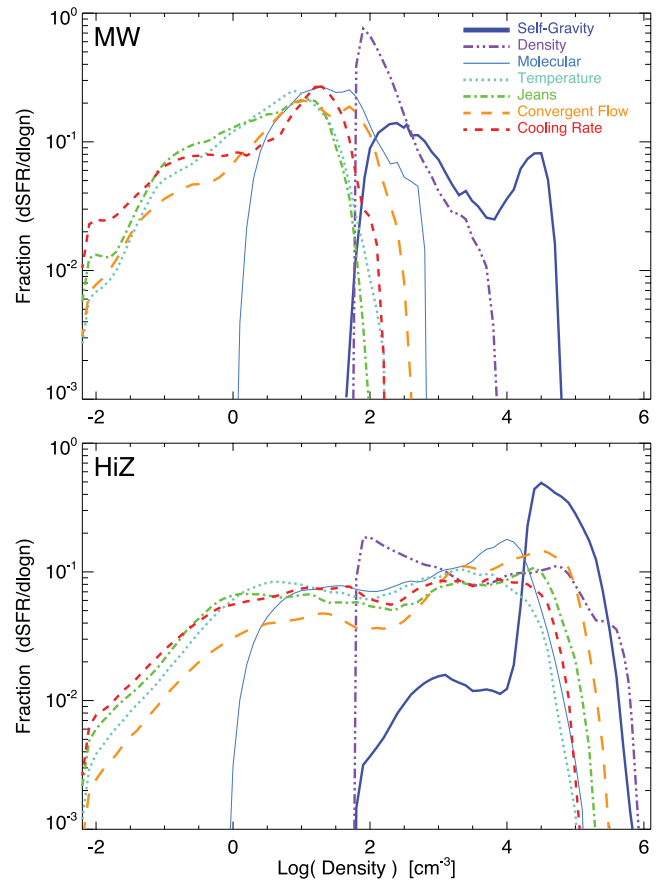


Figure 3. SFR-weighted density distribution for the simulations with different SF prescriptions (labelled) in the MW-like (top) and starburst/HiZ (bottom) disc models. The self-gravity criterion identifies the most dense regions. A fixed density threshold simulation is dominated by SF near the threshold, which is much lower than the maximum densities in the HiZ model. A molecular criterion effectively corresponds to a much lower threshold; for the metallicities here $\approx 1 \text{ cm}^{-3}$. The other criteria spread the SF across almost all the gas, even at very low densities.

selecting ‘overdensities’ at $\sim 1 \text{ pc}$ would require a threshold a factor of $\sim 10^9$ larger than the threshold at $\sim \text{kpc}$ – and the threshold we use on those scales is already much larger than the value chosen in most simulations!

Identifying SF with molecules (3) is reasonably similar to the choice of a high threshold density or self-gravity, when we focus on regions of very low mean surface density/opacity. When the average surface density is $\lesssim 10 M_{\odot} \text{ pc}^{-2}$ (at $Z \sim Z_{\odot}$), the medium is not self-shielding and becomes atomic dominated, so these criteria all similarly select overdense regions where rapid cooling has enabled collapse. But as soon as the density rises much above this value, the (dense) gas is essentially *all* molecular, and the criterion becomes meaningless (distributing SF equally among all gas). This ‘smears out’ SF in the dense gas, evident in Fig. 2 (which now appears as if it were effectively lower resolution). In fact, for metallicities of $\gtrsim 0.1 Z_{\odot}$, we see in Fig. 3 that this criterion is nearly identical to invoking a relatively low ‘threshold’ density of $n_0 \sim 1 \text{ cm}^{-3}$. At lower metallicities significant differences appear (Kuhlen et al. 2011), but there is almost no difference in an *instantaneous* sense between this model and a threshold density – the differences owe to the fact that at these metallicities cooling rates are sufficiently suppressed such that the cooling time is no longer short compared to the dynamical time (Glover & Clark 2012).

A temperature criterion (4), Jeans criterion (5) and rapid cooling criterion (7) identify the ‘molecular’ gas from criterion (3), but also include a wide range of gas at even lower densities. This can include e.g. adiabatically cooled gas in winds and cold clumps which have been shredded by feedback. As a result SF in Fig. 2 is effectively distributed over all the gas (clearly over several dex in Fig. 3, down to $n \sim 0.01\text{--}0.1\text{ cm}^{-3}$); the only reason it is concentrated towards the centre at all is because of the global concentration of gas mass.

An inflow/convergent flow criterion (6) has almost no effect on the distribution of SF, except to randomly select $\sim 1/2$ of the gas. This is because the medium is turbulent on all scales, so $\text{SIGN}(\nabla \cdot \mathbf{v})$ is basically random.

The binding energy criterion used here appears to have a number of advantages over the traditional fixed density threshold criterion for following SF in galaxy simulations. It is physically well motivated and removes the ambiguity associated with assigning a specific density – it also agrees well with the results of much higher resolution simulations of SF in individual local regions (Padoan et al. 2012). With realistic feedback models present, it is possible to set $\epsilon = 1$, i.e. have order-unity efficiency in bound regions, and correctly reproduce the observed SF efficiencies both globally and in dense gas. This removes the dependence of the observed Schmidt–Kennicutt relation on all resolved scales on the ‘by hand’ insertion of a specific efficiency. Interestingly, the total mass in dense ($n \gtrsim 100\text{ cm}^{-3}$) gas is similar in the runs with a density threshold and $\epsilon = 0.015$, and those with a self-gravity criterion and $\epsilon = 1$. In the latter case, a large fraction of the dense gas at any moment is not locally self-gravitating; the broad distribution of virial parameters in simulated GMCs is shown in Paper II, figs 17 and 18, and Dobbs, Burkert & Pringle (2011). So in this (local) sense as well as in the global average SFR shown here, the ‘average efficiencies’ emerge similarly. A more quantitative calculation of the dense gas distributions as tracers of the local SF efficiency is presented in Hopkins et al. (2012b).

Most importantly, the self-gravity criterion is inherently adaptive, and so allows for the simultaneous treatment of a wide dynamic range – critical for simulations of e.g. galaxy mergers, active galactic nuclei and high-resolution cosmological simulations. In these models, gas which is likely to be ‘star forming’ in one context (say a GMC in the outer parts of a galaxy disc) might be orders of magnitude below the densities needed for it to be even tidally bound in other regimes, so no single density threshold is practical for realistic simulation resolution limitations. For example, in the Milky Way, the central molecular zone is observed to have very high gas densities relative to the solar neighbourhood and even many GMCs, but is not strongly self-gravitating, and so appears to have an SFR far lower than what would be predicted by a simple density threshold argument (see Longmore et al. 2013).

Of course, it is possible to combine the criteria here, requiring self-gravity in addition to some density/temperature/molecular threshold, for example. However, based on our results, the addition of most of these criteria will not dramatically modify the results from a binding criterion alone. Moreover, it is not entirely obvious if they add physical information – at low densities, for example, one might posit that a region should not form stars unless it is also cold. But if it does not form stars (and so cannot be disrupted by feedback), it would collapse (if it could be resolved) to much higher densities, at which point it should eventually become cold and molecular as well. The exception is the cooling time criterion – rapid collapse implicitly assumes efficient cooling; it is less clear what will happen to a clump that is bound but cannot dissipate. Likewise, one may wish to adopt other criteria for non-bound regions. For exam-

ple, associating a low but non-zero efficiency even with unbound but turbulent regions above some density threshold, to represent the fact that there is an (unresolved) distribution of densities therein, some of which might be self-gravitating themselves (see e.g. Krumholz & McKee 2005; Hopkins 2012). We have experimented with such a prescription (with $\epsilon = 0.01$ for $n_{\text{crit}} > 100\text{ cm}^{-3}$), and find that the contribution from the unbound material is generally subdominant (but non-negligible).

Ultimately, testing which prescription is most accurate in simulations should involve direct comparison with observations. Since we have shown that the different simulation criteria are degenerate in their predictions of the total SFR and SF ‘efficiency’, this is not a good observational constraint to test the models. However, it is possible to measure how the observed SF in resolved galaxies is distributed with respect to the average gas density (or column density) on different *resolved* scales, essentially constructing a direct analogue of Fig. 3. The differences there and in the spatial distribution of SF in Fig. 2 should also be manifest in quantities such as the spatial correlation function of SF (and young stars), and the sizes of different star-forming regions (e.g. the characteristic sizes of the star-forming portions of spiral arms or GMC complexes). The behaviour of the local, small-scale SF law (as a function of density or other parameters) also ultimately informs the ‘subgrid’ physics what these models are intended to reproduce.

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