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Galaxy Zoo: comparing the demographics of spiral arm number and a new method for correcting redshift bias

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ABSTRACT

The majority of galaxies in the local Universe exhibit spiral structure with a variety of forms. Many galaxies possess two prominent spiral arms, some have more, while others display a many-armed flocculent appearance. Spiral arms are associated with enhanced gas content and star formation in the discs of low-redshift galaxies, so are important in the understanding of star formation in the local universe. As both the visual appearance of spiral structure, and the mechanisms responsible for it vary from galaxy to galaxy, a reliable method for defining spiral samples with different visual morphologies is required. In this paper, we develop a new debiasing method to reliably correct for redshift-dependent bias in Galaxy Zoo 2, and release the new set of debiased classifications. Using these, a luminosity-limited sample of ∼18,000 Sloan Digital Sky Survey spiral galaxies is defined, which are then further sub-categorized by spiral arm number. In order to explore how different spiral galaxies form, the demographics of spiral galaxies with different spiral arm numbers are compared. It is found that whilst all spiral galaxies occupy similar ranges of stellar mass and environment, many-armed galaxies display much bluer colours than their two-armed counterparts. We conclude that two-armed structure is ubiquitous in star-forming discs, whereas many-armed spiral structure appears to be a short-lived phase, associated with more recent, stochastic star-formation activity.

Key words: methods: data analysis – galaxies: formation – galaxies: general – galaxies: spiral – galaxies: structure.

1 INTRODUCTION

Spiral galaxies are the most common type of galaxy in the local Universe, with as many as two-thirds of low-redshift galaxies exhibiting discs with spiral structure (Nair & Abraham 2010; Lintott et al. 2011; Willett et al. 2013; Kelvin et al. 2014a). As star formation is enhanced in gas-rich disc galaxies (Schmidt 1959; Kennicutt 1989; Kelvin et al. 2014a) understanding spiral structure holds the key to understanding star formation in the local Universe, yet formulating a single theory to account for all spiral structure still remains elusive. The main theories for the occurrence of spiral arm features in local galaxies initially focused on the idea of being caused by density waves in their discs (Lindblad 1963; Lin & Shu 1964), but have since been superseded by theories that consider the effects of gravity and disc dynamics (Toomre 1981; Sellwood & Carlberg 1984), with most of the work to advance the field of spiral structure theory driven by simulation [e.g. Dobbs & Baba (2014) and references therein, and discussed further in Section 4]. Using observational studies to test these theories remains a challenge, as visual classifications of both the presence of spiral structure and details of its features are required, which are difficult to obtain when considering the large samples provided by galaxy survey data. An approach that has been successfully employed to visually classify galaxies in large surveys is citizen science, which asks many volunteers to morphologically classify galaxies rather than relying

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on a small number of experts. Sophisticated automated methods have also been developed for this purpose, (e.g. Huertas-Company et al. 2011; Davis & Hayes 2014; Dieleman, Willett & Dambore 2015). However, these methods cannot currently completely reproduce the results of visual classifications, particularly in low signal-to-noise images. They also require training sets, meaning that ‘by eye’ inspection methods are still a requirement. Galaxy Zoo 1 (GZ1; Lintott et al. 2008, 2011) was the first project to collect visual morphologies using citizen science, by classifying galaxies from the Sloan Digital Sky Survey (SDSS) as either ‘elliptical’ or ‘spiral’. Using this method, each galaxy is classified by several individuals, and a likelihood or ‘vote fraction’ of each galaxy having a particular feature is assigned as the fraction of classifiers who saw that feature. GZ1 classifications collected in this way have been used to compare galaxy morphology with respect to colour (Bamford et al. 2009; Masters et al. 2010a,b), environment (Bamford et al. 2009; Skibba et al. 2009; Darg et al. 2010a,b), and star-formation properties (Tojeiro et al. 2013; Schawinski et al. 2014; Smethurst et al. 2015).

Following from the success of GZ1, more detailed visual classifications were sought, including the presence of bars, and spiral arm winding and multiplicity properties. Thus, Galaxy Zoo 2 (GZ2) was created (Willett et al. 2013, hereafter W13), in which volunteers were asked more questions about a subsample of GZ1 SDSS galaxies. The main difference between GZ2 and GZ1 was that visual classifications were collected using a ‘question tree’ in GZ2, to gain a more exhaustive set of morphological information for each galaxy. GZ2 has already been used to compare the properties of spiral galaxies with or without bars (Masters et al. 2011, 2012; Cheung et al. 2013), look for interacting galaxies (Casteels et al. 2013), as well as looking for relationships between spiral arm structure and star formation (Willett et al. 2015). This ‘question tree’ method has since been used in a similar way to measure the presence of detailed morphological features in higher redshift galaxy surveys (e.g. Melvin et al. 2014; Simmons et al. 2014), and other ZOONIVERSE1 citizen science projects.

An issue that arises in both visual and automated methods of morphological classification is that detailed features are more difficult to observe in lower signal-to-noise images (i.e. observed from a greater distance). In Galaxy Zoo, this has been termed as classification bias. It is imperative that classification bias is removed from morphological data, as it leads to sample contamination from galaxies being incorrectly assigned to some categories. This means that any observational differences between samples can be significantly reduced.

Classification bias manifested itself in GZ1 with galaxies at higher redshift having lower ‘spiral’ vote fractions, which were corrected using a statistical method (Bamford et al. 2009). The application of a question tree in GZ2 to look for more detailed features means that correcting for biases is more complicated than in GZ1. In particular, there are questions with several possible answers, and debiasing one answer with respect to each of the others is therefore a more difficult process for GZ2.

The paper is organized as follows. In Section 2, the sample selection and galaxy data are described. In Section 3, we describe a new debiasing method that has been created to account for the classification bias in the GZ2 questions with multiple possible answers. In Section 4, samples of GZ2 spiral galaxies are defined and sorted by arm multiplicity. This is a case where the new debiasing method

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1 https://www.zooniverse.org/
on the full sample. The lower redshift limit avoids a small number of galaxies with very large angular sizes, and hence accompanying morphological, photometric and spectroscopic complications. The upper redshift limit also corresponds to that for which we have reliable galaxy environmental density data from Baldry et al. (2006), which we will make use of in this paper.

The luminosity-limited sample is incomplete for the reddest galaxies at \( \log(M/M_\odot) < 10.6 \) (calculated using the method in Bamford et al. 2009). Where necessary we therefore consider a stellar mass-limited sample of 41 801 galaxies, created by applying a limit of \( \log(M/M_\odot) \geq 10.6 \) to the luminosity-limited sample.

2.2 Stellar population models

In Section 4.2.4, we evaluate potential star-formation histories by comparing observed galaxy colours. Spectral energy distributions are derived from Bruzual & Charlot (2003), for a range of ages and SFHs using the initial mass function from Chabrier (2003). For star-forming galaxies in the SDSS, the mean stellar metallicity varies from \( Z \approx 0.7Z_\odot \) for \( M \sim 10^{10.6}M_\odot \) (the lower limit of the stellar mass-limited sample) to \( Z \approx Z_\odot \) for \( M \sim 10^{11}M_\odot \) (Peng, Maiolino & Cochrane 2015). As we expect most spirals to be blue star-forming galaxies (e.g. Bamford et al. 2009), we approximate the metallicity of the stellar mass-limited spiral sample using a metallicity value of \( Z = Z_\odot \). Two dust extinction magnitudes of \( A_V = 0 \) and \( A_V = 0.4 \) are considered (Calzetti et al. 2000). Equivalent colours for each of the star formation and dust extinction models are calculated for each of the SDSS ugriz filters (Doi et al. 2010). Full details of how the models are derived can be found in Duncan et al. (2014).

2.3 Quantifying morphology with Galaxy Zoo

In GZ2, morphological information for each galaxy was obtained by asking participants to answer a series of questions. The structure of this question tree is shown in Fig. 2. Typically, each image was viewed by \( \geq 40 \) people (W13), although no user will explicitly answer every question in the tree for a particular galaxy. To reach the questions further down the tree, it is required that another question has been answered with a specific response. For each question, the responses are each represented by the ‘vote fraction’ \( p \) assigned to each possible answer. For any given question, the sum of the vote fractions for all possible answers adds up to one. Considering the ‘edge-on’ question (T01 in Fig. 2), a classifier would only answer that question if they answered ‘features/disc’ for T00. For example; if a galaxy was classified by 40 people, and 30 of those said they saw features, whilst the other 10 claimed it was smooth, then the corresponding vote fractions are \( p_{\text{features}} = 0.75 \) and \( p_{\text{smooth}} = 0.25 \). Only the 30 classifiers who saw ‘features’ would then answer the ‘edge-on’ question (T11 of Fig. 2). If 15 of those said the galaxy was edge-on, and 15 said it was not, the corresponding vote fractions would be \( p_{\text{edge-on}} = 0.5 \) and \( p_{\text{not edge-on}} = 0.5 \).

In order to reduce the influence of unreliable classifiers, W13 downweighted individual volunteers who had poor agreement with the other classifiers. Throughout this paper we refer to these weighted vote fractions as the ‘raw’ quantities. Before using these GZ2 vote fractions to study the galaxy population, we must first consider the issue of classification bias, as we shall in Section 3.1.

Traditional morphologies assign each galaxy to a specific class, usually determined by one, or occasionally a few, experts. In contrast, Galaxy Zoo provides a large number of independent opinions on specific morphological features for each galaxy. This allows us to consider both the inherent ‘subjectiveness’ and observational uncertainties of galaxy morphology, and hence control the compromise between sample contamination and completeness.

There are two principal ways in which galaxy morphologies can be quantified using Galaxy Zoo vote fractions. The first is to consider means of the vote fractions over specific samples or bins divided by some other property. These average vote fractions can then be used to study variations in the morphological content of the galaxy population. Individual galaxies are not given specific classifications. There is no population of ‘unclassified’, and hence ignored, galaxies. This approach has been taken by Bamford et al. (2009), Castelles et al. (2013), Willett et al. (2015), and various other studies. With this method, the vote fractions of all galaxies can be considered together; even galaxies with a small (but non-zero) vote fraction for a given property count towards the statistics. Effectively, this approach considers the vote fractions as an estimate of the probability of a galaxy belonging to a particular class.

The second approach is to divide the galaxy sample into different morphological categories, either by applying a threshold on the vote fractions, or choosing the class with the largest vote fraction. Such methods have been used by Land et al. (2008), Skibba et al. (2009), Galloway et al. (2015) and many more. One advantage of this approach is that each galaxy is assigned to a definite class, with the threshold tuned to ensure a desired level of classification certainty. However, a set of ‘uncertain’ or ‘unclassified’ galaxies may remain. In some analyses these will require special attention.

These different approaches are also relevant for how questions at different levels in the tree are combined. For example, a participant is only asked if they can see spiral arms when they have already answered that they can see features in the galaxy and that the galaxy is not an edge-on disc. The vote fraction for spiral arms therefore represents the conditional probability of spiral arms given that features are discernible and that the galaxy is not edge-on. When considering whether a galaxy displays spiral arms, one should account for the answers to these previous questions in the tree. One can treat vote fractions as probabilities, multiplying them to obtain a ‘probability’ that a galaxy displays any features, is not edge-on and possesses spiral arms. Alternatively, one may select a set of galaxies that display features, are not edge-on and possess spiral arms, by applying some thresholds to the vote fractions for each question in turn. [See Castelles et al. (2013) for a more thorough discussion of these issues.]

The primary morphological feature we will focus on in this paper is the apparent number of spiral arms displayed by a galaxy. Some of the classes for this feature, though, contain a relatively low fraction of the total spiral population. In addition, the vote fractions for the preferred answer are often fairly low, with votes distributed over several answers. In such cases, averaging the vote fractions over the full sample does not work particularly well, as noise from more common galaxy classes overwhelms the subtle signal from rarer classes. In this paper, we therefore prefer to assign galaxies to morphological samples by applying a threshold or taking the answer with the largest vote fraction.

3 CORRECTING FOR REDSHIFT-DEPENDENT CLASSIFICATION BIAS

3.1 Biases in the Galaxy Zoo sample

Galaxies of a given size and luminosity appear fainter and smaller in the SDSS images if they are at higher redshifts. To correct for this, galaxy images in GZ2 are scaled by Petrosian radius (W13). As

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Figure 2. Diagram of the question tree used to classify galaxies in GZ2. The tasks are colour-coded by their depth in the question tree. As an example, the arm number question (T10) is a fourth-tier question – to answer that particular question about a given galaxy, a participant needs to have given a particular response to three previous questions (that the galaxy had features, was not edge-on and had spiral arms).
this means that galaxies at further distances are scaled to have the same angular size, their pixel resolution is lower. Detailed features can therefore be more difficult to distinguish in galaxies at higher redshift. As a result, visual galaxy classifications are biased, as fewer galaxies are classified as having the more detailed features at higher redshift, making a sample of galaxies with the these features incomplete.

It should be noted that such biases are not exclusive to Galaxy Zoo. Difficulty in detecting faint features in lower signal-to-noise galaxies is an inherent property of any visual or automated method of galaxy classification. The advantage of using Galaxy Zoo classifications is that they give a statistical method of measuring galaxy morphology. As each of the galaxies in the full sample has been visually classified by a number of independent observers, the apparent evolution in the presence of features can be modelled, and biases corrected accordingly.

Incompletecompleteness and contamination are defects that arise in a sample where an inherent redshift bias affects the classifications. Incompleteness affects the ‘harder to see’ features: the vote fractions for these features decrease with redshift, leaving us with poor number statistics for a sample we wish to define as having that feature. Contamination is the converse effect that appears in the ‘easier to see’ categories. For these responses, the vote fractions decrease with redshift, meaning that any samples defined using the Galaxy Zoo classifications will also include mis-classified galaxies that should have actually been included in one of the ‘harder to see’ categories. Any intrinsic differences between samples that one wishes to compare may therefore be negated.

The effect of redshift bias is shown in Fig. 3a, where the answer to the ‘smooth or features’ question is compared for high- and low-redshift samples. The redshift range of the SDSS sample is shallow enough to argue that there should be minimal change in the overall population of galaxies (Bamford et al. 2009; W13). In a luminosity-limited sample, the level of completeness should also be the same at all redshifts, meaning that the overall populations of the high- and low-redshift samples should be equivalent. However, Fig. 3a shows that the higher redshift vote fractions are dramatically skewed to lower values – generally, people are having greater difficulty in detecting the presence of features in the higher redshift images. Thus, there are fewer votes for galaxies showing ‘features’ and consequently more votes for galaxies being ‘smooth’. If one wished to compare a sample of galaxies with ‘features’ against one that is ‘smooth’ using the raw vote fractions, the number of galaxies with ‘features’ would be incomplete and the ‘smooth’ sample would be contaminated.

3.2 Previous corrections for redshift bias in GZ2

The previous debiasing procedure applied to both GZ1 and GZ2 focused on correcting the vote fractions of the galaxy samples by adjusting the mean vote fractions as a function of redshift. The method was first proposed in Bamford et al. (2009), and updated for GZ2 in W13. The method successfully adjusts the mean vote fractions for questions with two dominant answers, as can be seen from the vertical lines in Fig. 3b: the mean of the debiased high-redshift sample is much closer to the mean of the low-redshift sample than for raw vote distributions (Fig. 3a).

However, this technique has two limitations that make it unsuitable if we want to divide a galaxy sample into different morphology subsets. The first issue is that adjustment of the mean vote fraction does not necessarily lead to correct adjustment of individual vote fractions. This can be seen in Fig. 3b. Although the mean vote fraction for the high-redshift sample has been correctly adjusted to approximately match the low-redshift sample, the overall distribution does not. There is an excess of debiased votes in the middle of the distribution, and fewer votes for the tails of the distribution at $p \approx 0$ and $p \approx 1$. This effect is important if we wish to divide our sample into different subsets by morphological type. As the shape of the histograms is not consistent with redshift, the fraction of galaxies with $p_{\text{features}}$ greater than a given threshold can also vary with redshift.

As described in Section 2.3, GZ2 utilizes multiple answered questions to obtain more detailed classifications than GZ1. In cases where the votes are split between multiple categories, the debiasing method from W13 does not always adjust the vote fractions correctly. We show this effect for the ‘spiral arm number’ question (T10 of Fig. 2), in Fig. 4. A sample of ‘secure’ spiral galaxies with $p_{\text{features}} \times p_{\text{not edge-on}} \times p_{\text{spirals}} > 0.5$ is selected, (with the vote fractions corresponding to the debiased values from W13), and the mean vote fractions with respect to redshift for each of the arm number responses are plotted. A clear trend in $p_{\text{arm number}}$ is observed: the mean vote fractions vary systematically with redshift, even after the W13 correction has been applied. For this question, the answers with more spiral arms (3, 4, or 5+ spiral arms) are the ‘harder to see’ features meaning that there are fewer votes for these categories at higher redshift, which instead increase the 1 and 2 arm vote fractions. The 3, 4 and 5+ spiral arm samples of spiral galaxies therefore suffer from incompleteness. This is of particular importance in this case for two reasons. First, as this is a ‘fourth order’ question, as...
can be seen in Fig. 2, then the sample size is limited, as three questions must have been answered 'correctly' previously for a galaxy to be classified as spiral. Secondly, the 3, 4 and 5+ arm responses have low mean vote fractions overall, of $\lesssim 0.1$. Thus, the number statistics for these categories are very low, meaning they will suffer from high levels of noise. Correspondingly, the 1 and 2 armed spiral samples would suffer from contamination from galaxies that should have been classified as 3, 4 or 5+ armed.

### 3.3 A new method for removing redshift bias

Given the limitations described in Section 3.2, we attempt to construct a new method of debiasing the GZ2 data more effectively. When considering a question further down the question tree with low number statistics, such as the spiral arm question, we prefer to use a thresholding technique rather than using the weighted vote fractions (see Section 2.3 for a description of both methods). Using the arm number question as an example, the ‘2 spiral arms’ response dominates the overall vote fractions, making up $\sim 60$ per cent of the votes, as can be seen in Fig. 4. The rarer responses of 3, 4 or 5+ arms have much lower number statistics overall, with only $\sim 10$ per cent of the votes. The mean values can therefore be affected by the noise in the dominant category, which will be much larger than the noise for the rarer category. We therefore divide our galaxy sample into different sub-samples when comparing galaxies by spiral arm number.

Unlike the debiasing method in W13, our new method aims to make the vote distributions themselves as consistent as possible rather than purely aiming for consistency in the mean vote fraction values. As each galaxy is classified by 40 or more volunteers (W13), we have enough data to model the evolution of the vote distributions as a function of redshift. Different classifiers will have different sensitivity for picking out the most detailed features. Thus, as samples at higher redshift are considered, and hence with poorer image quality, we expect the vote fraction distributions to also evolve as some classifiers become less able to see the most detailed features. We aim to account for this bias by modelling the vote fraction distributions as a function of redshift, and correcting the higher redshift vote distributions to be as similar as possible to equivalent vote distributions at low redshift.

We first define samples of galaxies for each of the questions in turn. The sample is then binned in terms of the intrinsic galaxy properties of size and luminosity, and each of these bins is divided into redshift slices. We then attempt to model the vote distributions for each of the bins with respect to redshift, and thus match their distributions to those at low redshift. This means that if a vote fraction threshold is applied, the fraction of galaxies with a given feature remains constant: at each redshift, the sample is composed of the galaxies that are most likely to have that particular feature.

It must be noted that such a method could still be limited by small-number statistics, which is particularly common at higher redshifts. In the case that a feature’s vote fraction drops to 0, we cannot ‘add’ votes for a feature – it is only possible to debias the galaxies with $p > 0$, where there is evidence for a feature being present. This remains a problem for the categories where the vote fractions are lowest, such as in the responses to the odd feature question (T06 in Fig. 2).

#### 3.3.1 Sample selection for each question

As GZ2 morphologies are classified with a decision tree (see Section 2.3), not all of the questions were answered by each of the volunteers for a given galaxy. Answering the spiral arm number question is not appropriate for all of the galaxies in the sample: if a galaxy has no spiral features, yet a volunteer answered the spiral arm question, that galaxy would contribute ‘noise’ to the answers to that question. To avoid ‘noise’ introduced by incorrectly classified galaxies, clean galaxy samples are defined with $p > 0.5$. For the first question, this corresponds to all of the galaxies, as each classifier answered that particular question for each galaxy. However, when questions further down the tree are considered, this is not the case. The equivalent $p > 0.5$ for the spiral arm question would only include the galaxies with $p_{\text{features}} \times p_{\text{not edge-on}} \times p_{\text{spiral}} > 0.5$.

For each of the questions in turn, we define a sample of galaxies with which we will apply the new debiasing procedure. These samples are defined using a cut of $p > 0.5$ (corresponding to $p_{\text{features}} \times p_{\text{not edge-on}} \times p_{\text{spiral}} > 0.5$ for the spiral arm question for example). A further cut of $N \geq 5$ (where $N$ is the number of classifications) is also imposed to ensure that each galaxy has been classified by a significant number of people to reduce the effects of Poisson noise. In this case, the vote fractions must be the debiased vote values, to ensure each sample is as complete as possible (see Section 3.1) as we look at each question. The order in which the questions are debiased is important: to define a complete sample of galaxies to be used for the debiasing of a particular question, all questions further up the question tree must have been debiased beforehand.

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Figure 4. Mean vote fractions for each of the arm number responses to the ‘arm number’ question (T10 in Fig. 2). The sample consists of galaxies from the luminosity-limited sample, with $p_{\text{features}} \times p_{\text{not edge-on}} \times p_{\text{spiral}} > 0.5$ (with vote fractions taken from the W13 debiased catalogue). The solid lines show the mean arm number vote fractions obtained using the raw vote classifications, and the dashed lines indicate the same quantity obtained using the W13 debiased values. The shaded regions indicate the 1σ error on the mean.
It is expected that the ability to discern the presence of a particular feature will depend on intrinsic galaxy properties. For example, larger, brighter galaxies may be easier to classify over a wider redshift range. Conversely, fainter galaxies may show stronger features, as both overall galaxy morphology (Maller 2008; Bamford et al. 2009) and spiral arm morphology (Kendall, Clarke & Kennicutt 2015) have stellar mass dependences. To account for these possible variations, we bin the data in terms of $M_*$ and $\log (R_{\text{eq}})$ for each answer in turn. We use the voronoi_2d_binning package from Cappellari & Copin (2003), to ensure that the bins will have an approximately equal number of galaxies. Fig. 5 shows an example of the Voronoi binning for the 5+ arms response to the arm number question. When Voronoi binning the data for each of the answers, only the $N_{\text{gal}}$ galaxies with $p > 0$ are included, meaning that the ‘signal’ of galaxies is evened out over all of the Voronoi bins. We aim to have $\approx 30$ Voronoi bins for each of the questions, so the desired number of galaxies in each bin is given by $N_{\text{gal}}/30$.

After Voronoi binning the data in terms of their intrinsic properties of size and brightness, we further divide each bin into redshift bins, to allow us to study how the vote distributions change with redshift. Each redshift bin is constrained to contain $\geq 50$ galaxies. This binned data is used for the debiasing methods described in the next section.

### 3.3.3 Modelling redshift bias

For each of the possible responses to each question, a method is applied to correct for the redshift bias in the sample, aiming to make the vote distributions for each answer consistent with redshift. The two methods that we employ to achieve this are described below.

The first method we utilize to remove redshift bias simply matches the shapes of the histograms on a bin-by-bin basis. The cumulative distribution for the lowest redshift sample in a given Voronoi bin is used as a reference for how the shape of the histogram would look if it were viewed at low redshift. An example of this method is shown in Fig. 6, in which the ‘features or disc’ answer to the ‘smooth or features’ question is considered. For both the low-redshift bin and the high-redshift bin, the vote fractions are ranked in order of low to high. Each of the galaxies in the high-redshift bin is then matched to its low redshift equivalent by finding the galaxy with the closest cumulative fraction in the low-redshift bin. An example of this technique is shown by the vertical lines of Fig. 6. In this case, a galaxy with cumulative fraction of $0.2$ (corresponding to $p_{\text{features}} = 0.18$ and $p_{\text{arm}} = 0.65$) is matched to its low redshift equivalent by finding the galaxy with the closest cumulative fraction in the low-redshift bin. This is repeated for each galaxy and for each of the high-redshift bins in turn. Applying a vote fraction threshold for a given response gives the same fraction of the population above that threshold in all of the redshift bins, with the galaxies most likely to have a feature making up the population of galaxies above that threshold.

The main strength of this method is that any vote distribution can be modelled in this way, irrespective of the overall shape. However, a potential weakness is that noise can be introduced due to the discretization of the data. To limit this issue, each redshift bin has a ‘good’ signal of $\geq 50$ galaxies. This effectively ‘blurs’ any trends with redshift, and can actually lead to an overcorrection of vote fractions, which can be seen in Fig. 3c. Although the overall histogram shape is well matched when a slice at $0.08 \leq z < 0.085$ is considered, we see too many galaxies with $p \approx 1$ compared to the low-redshift data. This issue is purely caused by the discretization of the individual bins: although the trends can be modelled overall, any trends within individual bins cannot. If there is a redshift trend within a bin, then the fraction of galaxies with the more difficult
to see features will preferentially reside in the lower redshift ends of the bins. This effect leads to an overestimate of the number of galaxies with the more difficult to see features. Fig. 8a shows the debiased trends of the ‘features or disc’ question, which was debiased using the ‘bin-by-bin’ method, which shows that the method slightly overcorrects the redshift trend in the number of galaxies classified with $p > 0.5$.

One potential solution would be to bin the data more finely. However, there is no ‘ideal’ solution to this problem, as fewer galaxies in each bin would mean that the redshift range that each bin occupies is smaller, but the noise in each of the bins is larger.

To attempt to remove the discrete nature of the correction in the ‘bin-by-bin’ method, we use an alternative method that models the vote distributions with analytic functions. For each of the redshift bins, we plot a cumulative histogram of $\log(p)$ against the cumulative fraction. Examples of some of these cumulative histograms are plotted as the solid lines in Fig. 7. It can be seen that there is a clear evolution in the distributions with redshift. This effect is most prominent in the 4 and 5+ arms responses, where the distributions shift so that there are fewer galaxies with higher vote fractions. To correct for this bias, each of the cumulative histograms can be fitted to an analytic function, and the parameters of the function modelled in terms of redshift ($z$), galaxy size ($R_{50}$) and intrinsic brightness ($M_r$). After much experimentation, a function of the following form is used to model the cumulative distributions:

$$f(p) = e^{k_p c_p},$$

where $k$ and $c$ are variables fit to each of the curves. Best-fitting $k$ and $c$ values are found for each of the bins, indicated by the dashed lines in Fig. 7. When fitting, the cumulative histogram is sampled evenly in $\log(p)$ to avoid the fit being weighted to the steepest parts of the curves.

After finding $k$ and $c$ for each of the bins, we attempt to quantify how these parameters change with respect to $M_r$, $\log(R_{50})$ and $z$. A $2\sigma$ clipping is applied to all of the $k$ and $c$ values to remove any fits where discrepant $k$ or $c$ values have been found. The data are then fitted using a continuous function of the following form:

$$A_{\text{fit}}(M_r, R_{50}, z) = A_0 + A_M(f_M(-M_r)) + A_R(f_R(\log(R_{50}))) + A_z(f_z(z)),$$

where $A$ corresponds to either $k$ or $c$ and $f_M$, $f_R$ and $f_z$ are functions that can be either logarithmic ($\log x$), linear ($x$) or exponential ($e^x$). The values $A_0$, $A_M$, $A_R$ and $A_z$ are constants that parametrize the shape of the fit with respect to each of the terms. When fitting the data, $M_r$, $\log(R_{50})$ and $z$ correspond to their respective mean values calculated using all of the galaxies in that bin. The best combination of functions is chosen by calculating $A_0$, $A_M$, $A_R$ and $A_z$ for each combination of $f_M$, $f_R$ and $f_z$, and selecting the function that has the lowest squared residuals. We then clip any values with $a > 2\sigma$ residual to this fit and re-fit the data to find a final functional form for $k$ and $c$ with respect to $M_r$, $R_{50}$ and $z$. The resulting modelled cumulative histograms for the spiral arm number question are shown by the dotted lines of Fig. 7. Limits are also applied to $k$ and $c$ to...
Figure 8. Number of galaxies with $p > 0.5$ for each of the questions debiased using the method described in Section 3.3. The solid lines indicate the raw vote fractions and the dashed lines indicate the debiased vote fractions. The dotted lines indicate the same fractions using the W13 debiasing method. The total sample here is composed of galaxies in the luminosity-limited sample with $p > 0.5$ (as described in Section 3.3.1).

Avoid unphysical fits at extreme values of $M_R$, $R_{50}$, and $z$, set by the upper and lower limits of all of the fit $k$ and $c$ values within the $2\sigma$ clipping.

After finding a functional form for $k$ and $c$ with respect to $M_r$, log($R_{50}$), and $z$, each of the galaxies in the sample is debiased to find its equivalent value at low redshift. To do this for an individual galaxy, a cumulative histogram is estimated using $k_{\text{fit}}(M_r, R_{50}, z)$ and $c_{\text{fit}}(M_r, R_{50}, z)$, where $M_r$, $R_{50}$, and $z$ are the properties for that particular galaxy, giving the cumulative fraction for a galaxy's raw vote fraction. The equivalent cumulative histogram at $z = 0.03$ (the low-redshift limit of our luminosity-limited sample) is also found, using $k_{\text{fit}}(M_r, R_{50}, 0.03)$ and $c_{\text{fit}}(M_r, R_{50}, 0.03)$. The vote fraction for the corresponding cumulative fraction is read off from the low redshift cumulative histogram in a similar way as in the ‘bin-by-bin’ method, this time using the fitted curves rather than the raw histograms. This is repeated for each of the galaxies in the sample to generate a set of debiased values for the full sample of galaxies.

As mentioned previously, function fitting avoids issues related to the discretization of the data. However, it does introduce its own biases, as an assumption is made that the cumulative histograms can all be well-fitted by a particular set of continuous functions. This may not always be the case, so we must consider which of the above methods does the best overall job of removing redshift bias. To do this, the distributions of votes for a low-redshift reference sample are compared to the distributions of higher redshift bins. Using the luminosity-limited sample, which is free from redshift bias across all $M_r - R_{50}$ bins, a reference sample with $0.03 \leq z < 0.035$ is defined. The rest of the luminosity-limited sample is then split into 10 redshift slices, and the total square residual of the vote fractions from both of the debiased methods are calculated with respect to the raw vote distributions of the reference sample. The method with the lowest total square residual is used to compute the final debiased values.

3.3.4 Results from the new debiasing method

As described in Section 3.3, the new method aims to keep the fraction of galaxies above a given threshold constant with redshift, rather than simply correcting the mean vote fractions with redshift, as shown in Fig. 3c. To test how successful the new debiasing method is at defining populations of galaxies above a given threshold with redshift, the fraction of galaxies with $p > 0.5$ for each of the questions is plotted in Fig. 8. It can be seen that in most cases, the new debiasing method does keep the fraction of the population with $p > 0.5$ constant with redshift, as expected. This effect is most
Figure 9. Vote distribution histograms for each of the answers in the GZ2 question tree. The blue filled histogram shows the distribution for galaxies with $0.03 < z < 0.035$, which should have minimal redshift-dependent bias. The black solid, red dotted and red dashed histograms show the distribution of galaxies at $0.08 < z < 0.085$ using the raw, W13 debiased, and debiased data from this paper, respectively. All samples use only galaxies with $p > 0.5$ (as described in Section 3.3.1) from the luminosity-limited sample.

It can be seen that the original debiasing method does not adequately remove redshift bias, with fewer galaxies exhibiting spiral structure at higher redshift. However, our new method does keep this fraction approximately constant with redshift, which means the spiral sample will be more complete if we wish to use a thresholding technique to define a sample of galaxies with spiral structure.

Fig. 8 only shows the specific example of the threshold of $p > 0.5$. This does not give any insight into the overall vote fraction distribution, which can vary with redshift as shown in Fig. 3. Therefore, overall distributions are compared for two redshift slices in Fig. 9. It can be seen that this new method does not always ‘match’ the low- and high-redshift samples exactly, an effect that is most obvious in the ‘spiral’ question. Rather than getting an excess of votes towards the middle of the distribution, excesses are more generally seen at the tails of the distributions at $p \approx 0$ and $p \approx 1$. This is because our method preferentially matches the $p \approx 1$ end of the distribution. As can be seen by the ‘spiral = yes’ response in Fig. 9, the top ends of the distributions are usually correctly matched; the scarcity of votes for the intermediate values of $p$ are caused by the excess of galaxies with $p = 0$ that cannot be corrected.

3.4 Debiased data

The data from the new debiasing method described in this Section 3.3 is available from data.galaxyzoo.org. Alongside the raw vote fractions, our new debiased vote fractions are listed, as well as a gz2_class and flags for ‘securely’ detected spiral or elliptical galaxies.
galaxies (described in more detail in W13). A portion is shown in Table 1 to show the form and content of the data. The table includes the weighted counts and weighted fractions from W13, with our debiased vote fractions.

### 4 PROPERTIES OF SPIRAL GALAXIES WITH RESPECT TO ARM NUMBER

Despite how prevalent spiral galaxies are in the local Universe, formulating a single, complete picture as to how they form and evolve is still elusive. Spiral arms are associated with enhanced levels of gas density (e.g. Grabelsky et al. 1987; Elmegreen & Elmegreen 1987a; Engargiola et al. 2003), star formation (Seigar & James 2002; Grosbol & Dottori 2012) and dust opacity (Holwerda et al. 2005). One of the key reasons why this is the case is because spiral structure can take many varied appearances. Spiral galaxies are often classified using either their Hubble type (Hubble 1926) or an Elmegreen-type classification scheme (Elmegreen & Elmegreen 1982, 1987b). Using the Hubble method, spiral galaxies are assigned Hubble types depending on their bulge prominences and pitch angles. More detailed classification can be applied using the de Vaucouleurs classification scheme (de Vaucouleurs 1959, 1963), where the presence of more detailed structure such as diffuse, irregular spiral arms and rings can also be morphologically assigned. However, the Hubble-type classification scheme and its later revisions classify spiral galaxies by their bulge prominence and their spiral arm pitch angle. These properties are weakly related (Kennicutt 1981; Seigar & James 1998): spiral arm tightness has been shown to be more strongly correlated with bulge total mass (Seigar et al. 2008; Berrier et al. 2013; Davis et al. 2015), rather than bulge-disc ratio. The Elmegreen-type classifications scheme instead divides galaxies into different types depending on the spiral arm structure itself, rather than any properties related to the galactic bulge. This scheme generally classifies galaxies as one of three types: grand design, multiple-armed or flocculent. Grand design spiral structure is associated with two symmetric spiral arms, whereas multiple-armed structure is associated with more than two spiral arms and flocculent galaxies have many, shorter, less well-defined arms. The distinct advantage to classifying spiral galaxies in this way is that contrasting physical mechanisms are thought to play a role in the formation of these two different types of spiral structure.

Grand design spiral structure was initially thought to be due to the presence of a density wave in a galaxy’s disc (Lindblad 1963; Lin & Shu 1964), in which gas is ‘shocked’ into forming stars in regions of high density in the disc. However, this mechanism is no longer favoured, as there is no evidence for the enhancement of star formation in grand design spiral galaxies compared to many-armed spiral galaxies of the same stellar mass (Elmegreen & Elmegreen 1986; Dobbs & Pringle 2009), or any evidence for enhancement in star formation in the individual arms of such galaxies (Foyle et al. 2011; Choi et al. 2015). Instead, it is thought that grand design spiral structure may actually occur as a result of strong bars in galaxy discs or tidal interactions (Kormendy & Norman 1979). Early observational evidence supports the theory that grand design structure can be induced via interactions, with two-armed structure being favoured over many-armed structure in high-density environments (Elmegreen & Elmegreen 1982, 1987b; Ann 2014), and simulations showing that galaxy–galaxy interactions can lead to grand design spiral structure in galaxy discs like that seen in the local Universe (Dobbs et al. 2010; Semczuk & Lokas 2015).

Unlike two-armed spiral structure, many-armed spiral structure arises readily in simulations without the requirement for a trigger from either a bar instability or a tidal interaction (James & Sellwood 1978; Sellwood & Carlberg 1984). Such structures require a cooling of the gas in the disc to be sustained for long periods of time (Carlberg & Freedman 1985). More recent simulations, taking the disc gravity into account, have shown that ‘flocculent’ structure may actually be a transient feature of spiral galaxies, with spiral arms continually being made and destroyed (Bottema 2003; BABA et al. 2009; Grand, Kawata & Cropper 2012; Baba, Saioh & WADA 2013; D’Onghia, Vogelsberger & Hernquist 2013), rather than a long-lasting persistent structure. Despite the recent advances in the simulations of these disc galaxies, the picture as to how all of the processes shape spiral galaxies still remains unclear. Grand design spiral galaxies can still reside in low-density environments without the presence of bars (Elmegreen & Elmegreen 1982), meaning that they are not purely driven by these processes as described in Kormendy & Norman (1979). Additionally, the time-scales of the persistence of spiral structure is still unclear, particularly as older stellar populations viewed in the infrared show very different structure to the young stellar populations viewed at optical wavelengths (Block & Wainscoat 1991; Block et al. 1994; Thornley 1996). Most recent work on spiral structure have also mainly been focused on simulations of spiral structure. Putting observational constraints requires the visual inspection of the spiral arm structure in galaxy discs, so have been restricted to relatively small samples of order \( \leq 2000 \) galaxies (e.g. Elmegreen & Elmegreen (1982, 1989); Ann & Lee (2013)). We use the GZ2 vote classifications to compare the overall demographics of spiral structure in a much larger sample of SDSS galaxies, defining galaxy samples which are complete in both luminosity and stellar mass (see Section 2 for descriptions of how these samples are defined).
4.1 Spiral arms in Galaxy Zoo

In order to study how spiral properties vary, visual inspection of the number of arms in a spiral galaxy disc is required. Such classifications are provided by question T10 of the GZ2 question tree (see Fig. 2). This question has six possible responses. In this case, the responses will be referred to as $m$-values, and can take the value of either 1, 2, 3, 4, 5+ or ‘can’t tell’.

In order to compare different spiral galaxies, a secure sample of spirals must first be defined. The sample is defined by selecting galaxies with $p_{\text{features}} \times p_{\text{notedge-on}} \times p_{\text{spiral}} > 0.5$. A further cut is also imposed where only galaxies with $N_{\text{spiral}} - N_{\text{can't tell}} \geq 5$ are selected, meaning that at least five people classified the spiral arm number of each of the spiral galaxies, reducing the effects of noise due to low numbers of classifications. The population of galaxies selected in this way from the full sample will hereafter be referred to as the spiral sample. The samples defined using these same cuts from the luminosity-limited sample and stellar mass-limited sample are referred to as the luminosity-limited spiral sample and stellar mass-limited spiral sample.

Each galaxy is then assigned a specific spiral arm number $m$, of either 1, 2, 3, 4 or 5+ arms, depending on which response has the highest debiased vote fraction (excluding the can’t tell response). The debiased vote fractions for each of the arm number responses are hereafter referred to as $p_m$, where $m$ is either 1, 2, 3, 4 or 5+.

The debiasing procedure applied to this question has shifted the vote fractions for the multiple-armed ($m = 3, 4, 5+$) answers upwards overall, as can be seen in Fig. 10. This has the effect of making each of these samples more complete with redshift, and increasing their respective overall vote fractions. However, in the $m = 5+$ arms case, the sample is still somewhat incomplete, as the overall fraction of galaxies that are assigned to this category decreases with redshift. The vote fractions for $m = 5+$ fall to 0 far more quickly with redshift than any of the other categories, as can be seen from the dashed line in the bottom panel of Fig. 10, making the modelling of this redshift bias difficult. Despite this, the fraction of galaxies that make up the $m = 5+$ category are still significantly improved compared to the sample sizes that would be defined using either the raw vote fractions or the W13 debiased vote fractions, as can be seen in from the $N$ and $f$ columns of Table 2. Examples of some securely classified spiral galaxies are shown in Fig. 11, where each galaxy has a dominant vote fraction of $p_m > 0.8$. The samples of galaxies assigned to each of the different $m$-values are referred to as the arm number samples.

The main result of this debiasing is that galaxies with low vote fractions for the many-armed answers are included in the many-armed categories when they were not before. As a consequence, the population of $m = 2$ galaxies is less contaminated by galaxies that actually have 3, 4 or 5+ spiral arms. This effect is illustrated in Fig. 12, where a selection of spiral galaxies with $0.5 < p_m \leq 0.6$ are shown. It can be seen that the $m = 4$ and $m = 5+$ spiral samples at higher redshift include spiral galaxies that initially had much lower overall vote fractions. As an example, if one were to use the raw

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**Table 2.** Overall properties of galaxy populations with different numbers of spiral arms. The number of galaxies with 1, 2, 3, 4 and 5+ arms are shown for both the luminosity-limited and stellar mass-limited spiral samples. Mean stellar masses, colours and local densities are shown for each of the populations, with 1σ standard deviations indicated in parentheses. Errors on the mean ($\sigma/\sqrt{N_{\text{debiased}}}$) are all of order $<0.01$.

<table>
<thead>
<tr>
<th>$m$</th>
<th>$N_{\text{raw}}$</th>
<th>$f_{\text{raw}}$</th>
<th>$N_{W13}$</th>
<th>$f_{W13}$</th>
<th>$N_{\text{debiased}}$</th>
<th>$f_{\text{debiased}}$</th>
<th>$M_\star (\log(M/\text{M}_\odot))$</th>
<th>$g - i$</th>
<th>$\Sigma (\text{Mpc}^{-2})$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Luminosity-limited</td>
<td>12 554</td>
<td>1.00</td>
<td>14 297</td>
<td>1.00</td>
<td>17 957</td>
<td>1.00</td>
<td>10.62 (0.25)</td>
<td>0.82 (0.17)</td>
<td>−0.24 (0.56)</td>
</tr>
<tr>
<td>1</td>
<td>563</td>
<td>0.04</td>
<td>670</td>
<td>0.05</td>
<td>926</td>
<td>0.05</td>
<td>10.63 (0.28)</td>
<td>0.83 (0.19)</td>
<td>−0.25 (0.54)</td>
</tr>
<tr>
<td>2</td>
<td>9044</td>
<td>0.72</td>
<td>10 073</td>
<td>0.7</td>
<td>11 157</td>
<td>0.62</td>
<td>10.63 (0.24)</td>
<td>0.86 (0.17)</td>
<td>−0.21 (0.57)</td>
</tr>
<tr>
<td>3</td>
<td>1778</td>
<td>0.14</td>
<td>21 518</td>
<td>0.15</td>
<td>35 552</td>
<td>0.2</td>
<td>10.59 (0.26)</td>
<td>0.75 (0.15)</td>
<td>−0.28 (0.53)</td>
</tr>
<tr>
<td>4</td>
<td>615</td>
<td>0.05</td>
<td>751</td>
<td>0.05</td>
<td>1162</td>
<td>0.06</td>
<td>10.60 (0.26)</td>
<td>0.74 (0.15)</td>
<td>−0.30 (0.51)</td>
</tr>
<tr>
<td>5+</td>
<td>554</td>
<td>0.04</td>
<td>645</td>
<td>0.05</td>
<td>1160</td>
<td>0.06</td>
<td>10.65 (0.27)</td>
<td>0.75 (0.16)</td>
<td>−0.30 (0.53)</td>
</tr>
<tr>
<td>Stellar mass-limited</td>
<td>6683</td>
<td>1.00</td>
<td>7 226</td>
<td>1.00</td>
<td>9 413</td>
<td>1.00</td>
<td>10.81 (0.16)</td>
<td>0.91 (0.14)</td>
<td>−0.18 (0.57)</td>
</tr>
<tr>
<td>1</td>
<td>290</td>
<td>0.04</td>
<td>331</td>
<td>0.05</td>
<td>500</td>
<td>0.05</td>
<td>10.84 (0.16)</td>
<td>0.94 (0.14)</td>
<td>−0.19 (0.53)</td>
</tr>
<tr>
<td>2</td>
<td>4852</td>
<td>0.73</td>
<td>5 191</td>
<td>0.72</td>
<td>6 059</td>
<td>0.64</td>
<td>10.80 (0.15)</td>
<td>0.94 (0.13)</td>
<td>−0.15 (0.59)</td>
</tr>
<tr>
<td>3</td>
<td>886</td>
<td>0.13</td>
<td>991</td>
<td>0.14</td>
<td>1 654</td>
<td>0.18</td>
<td>10.82 (0.16)</td>
<td>0.83 (0.12)</td>
<td>−0.23 (0.53)</td>
</tr>
<tr>
<td>4</td>
<td>335</td>
<td>0.05</td>
<td>366</td>
<td>0.05</td>
<td>565</td>
<td>0.06</td>
<td>10.82 (0.16)</td>
<td>0.82 (0.12)</td>
<td>−0.25 (0.53)</td>
</tr>
<tr>
<td>5+</td>
<td>320</td>
<td>0.05</td>
<td>347</td>
<td>0.05</td>
<td>635</td>
<td>0.07</td>
<td>10.85 (0.18)</td>
<td>0.82 (0.13)</td>
<td>−0.26 (0.53)</td>
</tr>
</tbody>
</table>
Figure 11. Galaxies classified in each of the arm number categories \((m = 1, 2, 3, 4 \text{ or } 5+)\) for the stellar mass range \(10.0 < \log M_\ast/M_\odot \leq 11.0\). All of the galaxies are taken from the luminosity-limited spiral sample. Each galaxy has a debiased modal vote fraction \(p_m > 0.8\).

4.2 Comparing galaxy populations

Having defined the samples of spiral galaxies in Section 4.1, the demographics of the different galaxy populations separated by spiral arm number can be compared. For reference, mean stellar mass \((M_\ast)\), colour \((g - i)\) and local densities \([\Sigma, \text{ as described in Baldry et al. (2006); Bamford et al. (2009)}]\) are tabulated in the final three columns of Table 2.

4.2.1 Comparison of sample sizes

Spiral arm multiplicity does not map exactly to a specific Elmegreen-type for two reasons. First, the arm number itself does not give any indication of the prominence of spiral arms, so cannot be used to distinguish between a galaxy with many well-defined arms and one with more flocculent spiral structure, which are usually defined differently (Elmegreen & Elmegreen 1982, 1987b). The second issue is that arm structure may not necessarily be consistent at all radii (Grosbøl, Patsis & Pompei 2004) or at all wavelengths (Block & Wainscoat 1991; Block et al. 1994; Thornley 1996) within a galaxy disc, meaning that assigning a single \(m\)-value of arm number may not give a complete picture of the overall spiral arm structure. The most ‘easy-to-map’ categories may therefore be to compare the \(m = 2\) population with the galaxies classified as grand design, as grand design structure is usually associated with two well-defined arms across the entire disc (Elmegreen & Elmegreen...
Galaxies classified in each of the arm number categories \((m = 1, 2, 3, 4 \text{ or } 5+)\) for the stellar mass range \(10.6 < \log M_*/M_\odot \leq 11.0\). All of the galaxies are taken from the luminosity-limited spiral sample. Each of the galaxies is assigned to an arm number category by its modal \(p_{\text{m}}\) value. All of the modal \(p_{\text{m}}\)-values lie in the range \(0.5 < p_{\text{m}} \leq 0.6\).

In the luminosity-limited spiral sample, \(62.1 \pm 0.4\) per cent of the galaxies show two-armed spiral structure. This result is consistent with optical visual classifications (Elmegreen & Elmegreen 1982) and infrared classifications (Groshol et al. 2004), which suggest that \(\sim 60\) per cent of local spiral galaxies exhibit grand design spiral structure.

4.2.2 Stellar mass

Galaxy stellar mass is known to correlate with galaxy morphology (Bamford et al. 2009; Kelvin et al. 2014b), and spiral galaxy Hubble type (Muñoz-Mateos et al. 2015). It has been demonstrated that the central mass of spiral galaxies can play a role in the type of spiral structure exhibited in spiral galaxies. In particular, the pitch angle of spiral arms is related to both the star-formation rate in spiral galaxies (Seigar 2005), and the central mass concentration of the spiral galaxies (Seigar et al. 2006, 2014). Total galaxy stellar mass has also been found to correlate with observed spiral structure, with the strength of the \(m = 2\) mode in spiral galaxies being stronger in galaxies with greater physical size (Elmegreen & Elmegreen 1987b) and stellar mass (Kendall et al. 2015). In this section we will investigate whether the total galaxy stellar mass has any influence on the number of spiral arms in spiral galaxies.

The method for measuring stellar mass, described in Baldry et al. (2006), uses the \(u - r\) and \(M_r\) values from the SDSS. To avoid contamination of galaxies with uncertain stellar masses due to poor flux detection in these bands, only galaxies with \(F/\delta F > 5\) (where \(F\) is the flux error in a given band, and \(\delta F\) is the equivalent error on the flux) in both \(u\) and \(r\) are included in this analysis. The distributions of stellar mass for each of the arm number samples are shown in Fig. 13a. The overall distributions for each of the galaxy samples show that there is little evidence for a dependence of spiral
Figure 13. Left: distributions of stellar mass for the luminosity-limited spiral sample. The solid lines indicate the distributions for each of the arm number samples for each of arm numbers. The grey filled histograms show the equivalent distribution for all of the spiral galaxies for reference. The black dotted line indicates the stellar mass values above which the sample is complete in stellar mass. Right: fraction of the stellar mass-limited spiral sample classified as having each spiral arm number, in 20 bins of stellar mass. The shaded regions indicate the 1σ error calculated using the method described in Cameron (2011).

arm number with respect to host galaxy stellar mass; each of the samples contains galaxies across the entire range of stellar mass from $10.0 \lesssim \log(M_*/M_\odot) \lesssim 11.5$. A slight excess of low-stellar mass galaxies is found in the $m = 3$ and $m = 4$ samples, as well as an excess of high-stellar mass spiral galaxies for the $m = 5+$ sample.

The distributions of Fig. 13a show the distributions from the luminosity-limited spiral sample, so are therefore incomplete for galaxies with lower stellar masses (see Section 2.1) than $M_* \lesssim 10^{10.5} M_\odot$, indicated by the black dotted line. As we shall see in Section 4.2.4, lower mass galaxies are bluer, and hence more luminous for a given stellar mass. They are thus overrepresented at low masses in a luminosity-limited sample. To look for trends in terms of stellar mass, the overall fraction of the stellar mass-limited spiral sample is shown in Fig. 13b. Now, it can be seen that there do appear to be some trends between spiral arm number and host galaxy stellar mass. A significant increase in the fraction of galaxies with 5+ spiral arms is observed from the overall mean value of 0.068 ± 0.002 to 0.15 ± 0.02 for the highest stellar mass bin of $\log(M_*/M_\odot) = 11.2 \pm 0.1$. The $m = 3$ and $m = 4$ samples hint at similar, but much weaker trends. Conversely, the fraction of galaxies with two spiral arms decreases from 0.642 ± 0.004 for the total population to 0.53 ± 0.02 in the highest stellar mass bin.

One possibility why higher mass spirals may exhibit more spiral arms is that this could purely be an effect from the visual classifications. It has already been identified that the many-armed spiral features are the most difficult to detect, so may be more easily identifiable in the largest, brightest spiral galaxies. Spiral arms are already known to have greater amplitudes (i.e. be more prominent) in galaxies with larger stellar masses (Kendall et al. 2015). It has already been demonstrated in Section 3.3.4 that the $m = 5+$ sample is the most incomplete of the samples divided by spiral arm number. Thus, galaxies with greater stellar mass, that are therefore larger and brighter, may be preferentially put in this category, even after debiasing.

Another interesting scenario may be that the population of galaxies with the highest stellar mass are a population of unquenched spiral galaxies as in Ogle et al. (2016). Such galaxies still have their discs intact, so have no signatures of tidal interactions. As galaxy–galaxy interactions have been linked to both the inducement of two-armed spiral structure (Dobbs et al. 2010; Semczuk & Lokas 2015), and the depletion of gas and therefore quenching (Di Matteo et al. 2007; Lie et al. 2008), then one may conclude that the discs of these galaxies have not been disturbed. A possible explanation for this is that lower mass galaxies are more susceptible to environment effects (Bamford et al. 2009), so these discs are still forming stars in the transient way with multiple spiral arms, as described in Section 4.

4.2.3 Local environment

It is already well established that there is a clear dependence of the type of spiral structure that galaxies exhibit with respect to their local environment. Observational evidence from comparison of visually classified galaxies has found that grand design galaxies are more prominent in high-density group environments and in binary systems where a close companion galaxy is present (Elmegreen &
Elmegreen 1982, 1987b; Seigar, Chorney & James 2003; Elmegreen et al. 2011). These results suggest that a mechanism is responsible for the transformation of spiral structure as galaxies enter the highest density environments, with a plausible explanation being that two-armed spiral structure is the result of a recent gravitational interaction. N-body modelling of galaxies has shown that two-armed spiral structure can occur as a result of galaxy–galaxy interactions (Sundelius et al. 1987; Dobbs et al. 2010). However, the time-scales of the persistence of such structures are thought to be relatively short-lived (Oh et al. 2008; Dobbs et al. 2010), meaning that an enhancement in the fraction of grand design galaxies is only observed in the highest density environments where interactions can happen on a frequent enough basis to sustain such structures (Elmegreen & Elmegreen 1987b).

To compare spiral arm structure as a function of environment, a mean of $\Sigma_4$ and $\Sigma_5$ is used as an estimate of local density, as in Baldry et al. (2006); Bamford et al. (2009), denoted as $\Sigma$. $\log \Sigma$ is calculated as the mean of the density enclosed within the projected distance to the 4th and 5th neighbour and is hence an adaptive scale that probes both large scales outside groups and local scales within groups.

The distributions of galaxy local densities for each of the arm number samples are shown in Fig. 14a. Here, the stellar mass-limited spiral sample is used to define the total population, as $M_*$ and density are closely related (Baldry et al. 2006), so any biases in terms of the stellar mass distributions may have an effect on the completeness of the galaxy sample in terms of environment. The distributions show a modest dependence of spiral arm number with local density. However, as was the case for stellar mass, each of the arm number samples spans the entire range of local density defined by $\Sigma$.

The fraction of spiral galaxies which exhibit each of the spiral arm numbers as a function of $\log \Sigma$ are shown in Fig. 14b. A clear trend is observed, with the number of two-armed spiral galaxies increasing for the highest values of local density from 64.3 $\pm$ 0.5 per cent for the overall population to 75 $\pm$ 2 per cent for the highest density bin of $\log \Sigma = 1.1 \pm 0.2$. Conversely, all of the many-armed samples with $m = 3, 4$ or $5 +$ all show the opposite trends, with their respective fractions decreasing with $\Sigma$. These results therefore seem to be in qualitative agreement with Elmegreen & Elmegreen (1982) and Ann (2014), in which the fraction of galaxies displaying grand design spiral structure increases in the highest density environments. As the increase seems to be most distinct in the very highest densities, this could be indicative that two-armed spiral structure is a short-lived phase induced by galaxy–galaxy interactions, as described in Elmegreen & Elmegreen (1983). Interestingly, there is no clear enhancement in the fraction of galaxies with a single spiral arm at the highest densities, as found in Casteeles et al. (2013). However, Casteeles et al. (2013) found the most significant enhancements in $m = 1$ galaxies when galaxies have a close companion, which is not probed by our measure of environment. A more complete analysis of spiral structure with local environment, accounting for both interaction probabilities and local density will need to be considered to look for more significant trends of spiral arm structure with environment. With our large, clean samples of galaxies with measurements of arm number, we plan to take a more
4.2.4 Galaxy colours

Colours primarily indicate stellar population ages in galaxies, although dust extinction can also have an effect. Star-formation properties have been hypothesized to correlate with spiral arm properties, where galaxies with more prominent spiral arms show enhanced star formation (Seigar & James 2002; Kendall et al. 2015). The presence of a density wave in a galaxy disc has been proposed as a method of inducing star formation, but the lack of evidence for a clear enhancement of star formation in grand design spiral galaxies (Elmegreen & Elmegreen 1986; Foyle et al. 2010; Willett et al. 2015) or a clear age gradient within spiral arms (Foyle et al. 2011; Dobbs & Baba 2014; Choi et al. 2015) suggests that this is not the case.

Galaxy colour is already known to relate to stellar mass (e.g. Kauffmann et al. 2004; Baldry et al. 2006), environment (e.g. Kauffmann et al. 2004; Baldry et al. 2004 and overall galaxy morphology (e.g. Aaronson 1978; Glass 1984; Bamford et al. 2009). As spiral arms are associated with recent star formation, and also the presence of dust (Grosbol & Dottori 2012), we expect their properties to correlate with colour. Thus, galaxy colour correlates with the presence of spiral arms, with spiral galaxies being bluer in colour than ellipticals (Bamford et al. 2009; Schawinski et al. 2014). The colour distributions are now compared to look for any trends with recent star-formation history in Fig. 15a. The colours that are plotted here are the SDSS $g - i$ optical colours, which should probe recent star formation in galaxies. To avoid contamination from poor detections, only the galaxies with $F/δF > 5$ in both $g$ and $i$ are included. Unlike the distributions of local density and stellar mass, a strong trend is found between colour and arm multiplicity. The two-armed spiral galaxies show the reddest overall colours, with mean $g - i$ of 0.94 and a standard deviation of 0.13 in the stellar mass-limited spiral sample. The $m = 3, 4$ and $5+$ armed samples have corresponding colours of 0.83, 0.82 and 0.82, with corresponding standard deviations of 0.12, 0.12 and 0.13. Thus, each of the many-armed spiral samples is $\approx 1$ standard deviation bluer than the two armed spiral galaxy population.

As grand design spiral structure is associated with two spiral arms (Elmegreen & Elmegreen 1982), this red spiral galaxy population may be composed of strongly barred, grand design spiral galaxies.

To further compare the overall galaxy colours, the fraction of the stellar mass-limited spiral sample with each of the spiral arm numbers with respect to $g - i$ is shown in Fig. 15b. Here, a clear trend is observed with the fraction of galaxies displaying two spiral arms with respect to colour. In the bluest bin ($g - i = 0.67 \pm 0.07$), only $32 \pm 2$ per cent of galaxies have two spiral arms; in the reddest bin $g - i = 1.17 \pm 0.05$), $84 \pm 2$ per cent have two spiral arms.

As described above, a strong dependence of colour with stellar mass is well-known (e.g. Baldry et al. 2006). However, as described in Section 4.2.2, our samples only show very weak trends with stellar mass. To test whether any of the colour differences between the samples can be attributed to differences in stellar mass, $g - i$
colour is plotted against stellar mass in Fig. 16. The results show that the colour differences cannot be explained by the stellar mass differences between our arm number samples: for a given stellar mass, the many-armed spiral galaxies are much bluer in the $g - i$ band. The samples were also matched in terms of stellar mass, and the mean and standard deviations are indicated by the arrows in Fig. 15. The colour differences are still $\approx 1$ standard deviation bluer in the many-armed spirals compared to the two-armed spirals, after matching the samples by stellar mass.

Using a single colour only gives a broad indication as to how the star-formation properties of galaxies differ. To try to gain a more detailed understanding of the star formation in each of the arm number samples the $u - r$ and $r - z$ bands are compared for each of the different arm numbers, and the results are plotted in Fig. 17. Similar cuts in $F/5F$ to the $u$, $r$ and $z$ bands as described in Section 4.2.2 are used to define the samples. It can be seen that the differences are stronger in $r - z$ than in $u - r$. The most significant differences are observed between the $m = 2$ and $m = 5 +$ samples, where there is a significant offset in $r - z$ for a given $u - r$.

In order to gain an insight into how star formation can have affected the galaxy colours, the $m = 2$ and $m = 5 +$ $u - r$ versus $r - z$ distributions are plotted in Fig. 18, with $\tau$-model SFHs for reference from Bruzual & Charlot (2003) (see Section 2.2 for details). The SFH models are for a quenching galaxy, defined with two parameters, $t$ and $\tau$, where $t$ is the time of quenching onset and $\tau$ is the quenching time-scale (a shorter $\tau$ means a faster quenching). For each of the three time-scales, the dust extinction $A_V$ is set to 0. The plot indicates that both populations are consistent with SFH model

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Figure 16. Stellar mass versus $g - i$ colour galaxy samples classified by spiral arm number in the luminosity-limited sample. The black dotted line indicates where the sample is incomplete in terms of stellar mass. The grey-scale shaded contours show the total stellar mass-limited sample for all morphologies, whereas the solid lines show the distributions for each arm number sample. The contours are plotted with a kernel density estimate, of bandwidth optimized using 5-fold cross validation, and the selected bandwidths are displayed in the bottom-right corner of each plot. The contour levels show the regions enclosing 20 per cent, 40 per cent, 60 per cent, and 80 per cent of the points.

Figure 17. $u - r$ versus $r - z$ colours for each of the arm number samples taken from the stellar mass-limited spiral sample. The grey-scale shaded contours show the entire stellar mass-limited sample, irrespective of morphology, whereas the solid lines indicate the same distribution for each arm number sample. Contours are plotted using a kernel density estimate, with bandwidths optimized using 5-fold cross validation. The selected bandwidths are displayed in the bottom-right corner of each plot. The contour levels show the regions enclosing 20 per cent, 40 per cent, 60 per cent, and 80 per cent of the data for each sample.

Figure 18. Contour plots for the $m = 2$ (red solid contours) and $m = 5+$ (blue filled contours) samples as in Fig. 17. Three evolutionary tracks for Bruzual & Charlot (2003) stellar population models with different quenching time-scales ($\tau$) are plotted in black, yellow and green lines, indicated in the plot legend. Each point is coloured by the relative age of the SFH models ($t$), indicated in the colourbar. The green arrow indicates how the evolutionary curves would change colours with dust extinction $A_V$. 

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colours, but that the quenching process is much longer in the \( m = 2 \) population (indicated by a longer \( r \) ) than in the \( m = 5 \) population. The \( m = 5 \) population has therefore undergone a shorter, more recent phase of star formation. We also see a significant population of galaxies that are red in \( u - r \) and blue in \( r - z \), which cannot be explained by a \( t \) -model, even with a quickly declining SFR. A model with a recent, short burst superimposed on a longer, smoother SFH may be more suitable.

The role of dust must also be considered. A reference dust attenuation of \( A_v = 0.4 \) is shown by the green arrow of Fig. 18. The arrow indicates that extinction by dust could account for some of the differences in the colours of the galaxies if the attenuation is higher in the \( m = 2 \) population than the \( m = 5 \) population. However, such a scenario would seem unlikely, as dust opacity is greater within spiral arms (Holwerda et al. 2005). Therefore, one would expect that the spiral galaxies with more spiral arms to have a greater level of dust attenuation overall. Galaxies with greater levels of dust attenuation are also expected to have lower SFR (Garn & Best 2010), with the most passive spiral galaxies being the most dust deficient (Rowlands et al. 2012). It is therefore unlikely that dust attenuation in spiral galaxies could play a significant role unless the SFRs of two-armed spiral galaxies are significantly enhanced, which is not found to be the case (Willett et al. 2015).

Recent simulations of discs in spiral galaxies have proposed that flocculent spiral structure can be sustained for long periods of time, of order \( > 10 \) Gyr, (Fujii et al. 2011; D’Onghia et al. 2013), with spiral arms being frequently made and broken. Our results suggest instead that flocculent spiral structure is a short-lived phase, associated with a recent star-formation event. Simulations frequently model discs in isolation, so may not account for all processes, e.g. the effects that environment can have on the induction or transformation of the spiral structure in local galaxies.

To gain a more complete understanding of the effects of dust and star formation with respect to spiral arm number, further SFH models will be explored in a later paper. SFH models with more than a single component will be considered, as well as how the presence of bars and gas content affect the SFHs of the different galaxies.

5 CONCLUSIONS
In this paper, the demographics of local spiral galaxies have been compared with respect to spiral arm number, in order to gain an understanding of any significant differences in the physical processes responsible for their spiral structure. We make use of visual classifications of SDSS galaxies from GZ2. In order to obtain complete and clean samples, we have developed a new method to account for redshift-dependent bias. This corrects the vote fractions to ensure sample completeness, and avoid contamination between separate classes of galaxies. The method will also be applicable to further studies of Galaxy Zoo data, and potentially other citizen science projects.

A new debiasing method has been developed to remove the effects of redshift-dependent classification bias in Galaxy Zoo data. The method was required for the multiple-answer questions in Galaxy Zoo, where the previously defined debiasing method did not effectively remove redshift bias, leading to sample contamination from incorrectly classified galaxies. In this paper, we studied the arm-number question, which is a multiple-answer question, where the rarer many-armed samples were incomplete, and the two-armed category suffered from sample contamination. The new method was successful in making the samples more complete with redshift in this case.

Using the resulting classifications, the distributions of environment, stellar mass and colour were compared for spiral galaxies with different numbers of arms. We found that the most massive galaxies favour many-armed spiral structure, which may be indicative that their discs have not have been sufficiently perturbed to induce two-armed spiral structure. An enhancement in the fraction of two-armed spiral galaxies was observed in the highest density environments, indicating that galaxy–galaxy interactions could play a role in the inducement of two-armed spiral structure. By comparing optical colours, we find that two-armed galaxies are much redder in colour than galaxies with many spiral arms. Although many-armed spiral galaxies display similar \( u - r \) colours, the \( r - z \) colours are distinctly redder in the two-armed galaxy population. These colours are indicative of a recent, rapidly quenched (\( < 0.1 \) Gyr) burst of star formation, suggesting that many-armed spiral structure is a short-lived phase in galaxy discs, whereas star formation in two-armed spiral structure persists over much longer time-scales.

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Cross validation and kernel density methods made use of scikit-learn (Pedregosa et al. 2011) and astroML (Vanderplas et al. 2012). This publication made extensive use of the scipy Python module (Jones et al. 2001(8)), including the scipy.optimize module for curve fitting and minimization. This research also made use of Astropy, a community-developed core Python package for Astronomy (Astropy Collaboration et al. 2013).

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